Mitigation of ICI Through Optimized SSR ICI Self Cancellation Scheme in OFDM

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Abstract: Orthogonal frequency division multiplexing (OFDM) is extensively used in wireless communication systems because it offers high data rates and provides a better solution to inter symbol interference (ISI) caused by a multipath channel. A well-known problem of OFDM system is sensitivity to carrier frequency offset (CFO) and preventing interference between the subcarriers. In OFDM, high-rate data streams are divided into N parallel lower rate streams which are mapped by QAM or QPSK onto mutually overlapping subcarriers and transmitted simultaneously. Therefore, high rate bit stream is split into N parallel lower rate bit streams and each of these streams are modulated using one of N orthogonal sub-carriers. However, OFDM is being widely used in many applications such as IEEE 802.11a, the multimedia mobile access communication (MMAC), HIPER-LAN/2, Digital Video Broadcasting (DVB) and so on. In a basic communication system, the input data is modulated using only one carrier frequency. Therefore, the available channel bandwidth is totally occupied by each symbol. This type of mechanism can lead to inter symbol-interference (ISI) in frequency selective channels.

By inserting Guard interval with the cyclic extension of the OFDM symbol, the inter symbol interference (ISI) can be easily avoided. A well known problem with OFDM is its vulnerability to slight differences in frequency at the transmitter and receiver, normally referred as frequency offset, caused by Doppler shift due to relative motion between the transmitter and receiver. This carrier frequency offset (CFO) causes distort orthogonality between sub-carriers, which implies inter-carrier interference (ICI). There is one more deleterious effect caused by frequency offset is the redution of signal amplitude or peak in the output of the filters. The unwanted ICI causes leakage of power among subcarriers and it eventually degrades the Bit error Rate (BER) performance of the OFDM receiver. In the presence of ICI, it is very difficult to obtain the theoretical BER and CIR. The BER of the received signals are very sensitive to Doppler effects and frequency offsets.

Keywords: OFDM, ICI, ISI, CFO, CIR, BER, QAM

I. INTRODUCTION

In Today’s world OFDM plays vital role in wireless communication systems, which is a promising modulating technique for high data rate transmission in wireless communication systems. OFDM is a form of multi-carrier modulation technique [1], which effectively utilizes the spectrum by spacing the channels much closer together. This spectral efficiency can be achieved by making orthogonality between the sub carriers and preventing interference between the subcarriers. In OFDM, a high-rate data stream is divided into many lower-rate streams which are mapped by QAM or QPSK onto mutually overlapping subcarriers and transmitted simultaneously. Therefore, high rate bit stream is split into N parallel lower rate bit streams and each of these streams are modulated using one of N orthogonal sub-carriers. However, OFDM is being widely used in many applications such as IEEE 802.11a, the multimedia mobile access communication (MMAC), HIPER-LAN/2, Digital Video Broadcasting (DVB) and so on. In a basic communication system, the input data is modulated using only one carrier frequency. Therefore, the available channel bandwidth is totally occupied by each symbol. This type of mechanism can lead to inter symbol-interference (ISI) in frequency selective channels.

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II. LITERATURE SURVEY

OFDM

In an OFDM system, the input bit data stream is multiplexed into N symbol streams, each with T symbol period and each stream is modulated parallelly on synchronous sub-carriers. The discrete time OFDM symbol after the IFFT block at the transmitter can be written as
\[ x[n] = \frac{1}{N} \sum_{k=0}^{N-1} X(k) e^{j2\pi mk/N}, \ n = 0,1,2 \ldots N - 1 \] (1)

Where N is no. of subcarriers and X(k) denotes the modulated data symbol transmitted (M-ary phase-shift keying :BPSK,QPSK,QAM) on k\textsuperscript{th} subcarrier. Due to frequency offset and AWGN channel, the received OFDM signal can be expressed as

\[ y[n] = x[n] e^{j2\pi \delta n/N} + z[n], \ n = 0,1,2 \ldots N - 1 \] (2)

Where \( \delta \) represents the frequency offset obtained by calculating the frequency spacing between two subcarriers and z[n] is a zero-mean AWGN. The frequency domain signal at the k\textsuperscript{th} subcarrier with frequency offset after the Fast Fourier transform (FFT) block is given as

\[ Y[k] = X[k]S(0) + \sum_{m=0,m\neq k}^{N-1} X(m)S(m-k) + Z(k) \] (3)

Where Z(k) is k\textsuperscript{th} sample DFT of z(n) and the term S(m-k) is the ICI weighting coefficient between k\textsuperscript{th} and m\textsuperscript{th} subcarriers, which is given as

\[ S(m-k) = e^{j\frac{\pi(m+\delta-k)(1-\delta)}{N}} \frac{\sin[\pi(m+\delta-k)/N]}{\sin[\pi(m-k)/N]} \] (4)

Carrier-to-Interface Ratio (CIR) is defined as the ratio of the desired signal power to the power in the interference component. It serves as a good indication of signal quality. A channel with constant CFO, CIR is improved more than 15dB for group size is two. The desired signal is transmitted on at k\textsuperscript{th} subcarrier, then the CIR of Normal OFDM systems is simplified as:

\[ \text{CIR} = \frac{E[|I(k)|^2]}{E[|I(k)|^2]^2} = \frac{\sum_{m=1}^{N-1}|S(m)|^2}{\sum_{m=1}^{N-1}|S(m)|^2} \] (5)

CIR is a function of N and \( \delta \).

**PHASE SHIFT KEYING:**

The M-PSK modulation technique includes BPSK, QPSK, 16-PSK. At the transmitter section, the input bit data is first encoded by the channel to decrease the probability of error at the receiver. In BPSK constellation \( \text{dmin} = 2A \) and \( \text{yb} \) is defined as \( \text{Eb}=\text{N0} \) and sometimes it is called SNR per bit. With this definition we have:

\[ \text{yb} = \frac{\text{Eb}}{\text{N0}} = \frac{\text{dmin}^2}{4\text{N0}} \] (6)

For BPSK modulation technique, the theoretical equation for bit error rate (BER) in Additive White Gaussian Noise (AWGN) channel is

\[ \text{Pb} = Q(\sqrt{2\text{Eb}}) \] (7)

Where \( Q \) is a Gaussian function.

For MPSK signaling, we can easily calculate an approximation of BER using nearest neighbor approximation. The bit error probability can be approximated by:

This approximation is only good for high SNR.

**QAM** is a combination of amplitude and phase shift keying, which is extensively used as a modulation technique in digital telecommunication system. In QAM, high spectral efficiencies can be achieved by considering a suitable constellation size.

Bit error probability for MQAM can be approximated as

\[ \text{Pb} = \frac{2}{\log_2 M} Q\left(\sqrt{\frac{3\text{yb}\log_2 M}{M-1}}\right) \] (9)

**Advantages of MQAM over MPSK**

i. FOR MPSK, the signal constellation is circular, where as for MQAM it is rectangular.

ii. The bandwidth requirement of QAM is same as MPSK, but d_{MQAM}>d_{MPSK} for same transmitted power. Hence, QAM gives superior performance than that of MPSK.

iii. superior performance of MQAM can be realized only if the channel is free from nonlinearity(\because \text{amplitude variation is required for M-QAM})

**ICI REDUCTION METHODS**

Several ICI self cancellation methods were proposed in the literature during last few decades.

**A. ICI Self Cancellation Method**

ICI self cancellation scheme proposed by Zhao utilizes data allocation and combining of (1,-1) on two adjacent subcarriers [4] i.e., same data is modulated at k\textsuperscript{th} and k+1\textsuperscript{th} subcarriers using (1,-1) as data allocation and are grouped at the receiver with coefficient weights 1 and -1. However, its performance degrades at higher values of \( \delta \).

**B. Conjugate Cancellation**

Conjugate Cancellation had been proposed by Yeh, Chang and Hassibi. In this scheme, OFDM signal & its conjugate are multiplexed, transmitted and grouped at the receiver to reduce the effect of ICI [5]. However, its performance decreases as \( \delta \) increases. At higher \( \delta > 0.25 \), its CIR performance is aggravate than standard OFDM system.

**C. Phase Rotated Conjugate Cancellation (PRCC)**

Phase Rotated Conjugate Cancellation (PRCC) is an extension to conjugate cancellation, in which the phase is multiplied with the generated symbol and its conjugate signal to be transmitted over multiple paths [6]. Here the phase depends on \( \delta \) and hence it needs continuous (CFO) estimation and feedback circuitry, which ultimately increases the complexity of the hardware.

**D. Symmetric Symbol Repeat ICI Self Cancellation**

This method proposed by Sathanantham, Rajatheva and Slimane, which utilizes data allocation and combining of (1,-...

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1) at $k^{th}$ and (N-1-k)th subcarrier [7]. This scheme shows better CIR performance than ICI self cancellation scheme.

For the majority of subcarriers the difference between symmetrically placed ICI components is small (almost negligible). Therefore if a complex data pair ex: (a,-a) is modulated on a pair of two symmetrically placed subcarriers, then the ICI generated by these orthogonal subcarriers will be cancelled out. In this method the data symbol to be transmitted at the $k^{th}$ subcarrier is repeated at (N-1-k)th subcarrier with opposite polarity [8], i.e.,

$$X(N-1) = -X(0), ... X(N-1-k) = -X(k)$$

(10)

The received data signal at the $k^{th}$ subcarrier and (N-1-k)th subcarrier is given by

$$Y'(k) = \sum_{m=0}^{N-1} X(m) (S(m-k) - S(m+1-k)) + Z(k)$$

(11)

$$Y'(N-1-k) = \sum_{m=0}^{N-1} X(m) (S(m+k+1-N) - S(k-m)) + Z(N-1-k)$$

(12)

Where the ICI coefficient is given by

$$S'(m-k) = S(m-k) - S(m+1-k)$$

(13)

At the receiver section, each signal at the N-1-kth subcarrier is multiplied by “-1” and then added with the one at the kth subcarrier

$$Y''(k) = Y'(k) - Y'(N-1-k)$$

(14)

$$Y''(k) = \sum_{m=0}^{N-1} X(m) [(S(m-k) - S(N-1-m-k) - S(m+1-k-N) + S(k-m)) + Z(k)] - Z(N-1-k)$$

(15)

Thus CIR of conventional SSR ICI self cancellation scheme can be written as

$$\text{CIR} = \frac{|2S(0) - S((N-1-2k)) - S(1(N+2k))|^2}{\sum_{m=0,k}^{N-1} (S(m-k) - S(N-1-m-k) - S(m+k+1-N) + S(k-m))]^2}$$

(16)

**III. PROPOSED METHOD**

**System model**

![Fig 1: Block diagram of proposed scheme](image)

This paper deals with the improvement of previous methods and this method is an extension of SSR ICI Self-Cancellation technique.

Aim of the system model is to reduce the effect of ICI on OFDM by ICI modulation and ICI demodulation processes, without increasing the hardware complexity while maintaining bandwidth efficiency. The system model comprises of an OFDM transceiver that works in following steps: BPSK (or) QAM, Serial to Parallel Conversion, ICI SC Demodulation, IFFT, Add CP, parallel to serial converter followed by channel, Remove CP, FFT, ICI SC demodulation and BPSK (or) QAM demodulation.

In general at the transmitter a data allocation $(1,\lambda)$ is used at symmetrical placed subcarriers i.e.,

$$X(N-1) = -\lambda X(0), ... X(N-1-k) = -\lambda X(k)$$

(17)

Now the received data at the $k^{th}$ subcarrier and (N-1-k)th subcarrier is

$$Y'(k) = \sum_{m=0}^{N-1} X(m) (S(m-k) - \lambda S(m+1-k)) + Z(k)$$

(18)

$$Y'(N-1-k) = \sum_{m=0}^{N-1} X(m) (S(m+k+1-N) - \lambda S(k-m)) + Z(N-1-k)$$

(19)

So the received data with combination of $k^{th}$ and (N-1-k)th subcarriers with $(1,\mu)$

$$Y''(k) = Y'(k) - \mu Y'(N-1-k)$$

(20)

$$Y''(k) = \sum_{m=0}^{N-1} X(m) [(S(m-k) - \lambda S(N-1-m-k) - \mu S(m+1-k-N) + \lambda \mu S(k-m)) + Z(k)] - \mu Z(N-1-k)$$

(21)

Thus the CIR of the proposed scheme is

$$\text{CIRp} = \frac{\sum_{m=0,k}^{N-1} |\mu S(m-k) - \lambda S(N-1-m-k) - \mu S(m+k+1-N) + \lambda \mu S(k-m)) + Z(k)|^2}{\sum_{m+k}^{N-1} |\mu S(m-k) - \lambda S(N-1-m-k) - \mu S(m+k+1-N) + \lambda \mu S(k-m)|^2}$$

(22)

The optimal values $\lambda$ and $\mu$ have been found by using a technique known as Nelder Mead Simplex Algorithm (NMSA) [9]. These optimal values are calculated for at a very small interval of which results in maximize the CIR for given $\delta$. But the drawback is for every $\delta$, there are unique optimal values and always this needs a continuous CFO estimation, which increases the system complexity. For each pair of optimal values the CIR has been calculated which forms a matrix [8] i.e., the elements in the matrix as the form like CIRp ($\delta\nu$, $\lambda\nu$, $\mu\nu$)

$$v = \frac{\delta h - \delta \nu}{\sqrt{\delta}} + 1$$

(23)

$\delta h$ and $\delta \nu$ are highest and the lowest possible values respectively and $\sqrt{\delta}$ is normalized frequency offset. Here $\delta h = 0.25$ and $\delta \nu = 0.03$ and $\sqrt{\delta} = 0.02$ so that $v = 12$ to avoid the above drawbacks sub-optimal pair ($\lambda s o$, $\mu s o$) is considered by using the following criterion
\[ \lambda_{so,\mu_{so}} = \max_{\lambda_0, \mu_0} \left[ p - \frac{\sum_{j=1}^{p} (p-CIR(\delta, \lambda_0, \mu_0))}{v} \right] \] (24)

Where \( p \) is the maximum CIR of a particular row of the matrix and second term is mean deviation of the CIR of that row from the peak (\( p \)) of that row, here these sub-optimal values (\( \lambda_{so}, \mu_{so} \)) are independent of \( \delta \) in the proposed method. These values are. \( \lambda_{so}=0.6164 \) and \( \mu_{so}=1.0351 \)

IV. SIMULATION RESULTS

Here we have considered an OFDM system with \( N=64 \) subcarriers and BPSK or QAM technique is used to modulate each of the subcarrier. The simulation using MATLAB software are performed to evaluate CIR and BER performance. The proposed scheme cancels the ICI coefficient effectively and further improves the system throughput performance as shown through extensive simulations.

V. CONCLUSION

In this paper several ICI minimization methods are studied and reviewed. It will be shown that our approach gives better results than previous reduction methods. Moreover, we propose to perform the signal processing only on the transmitter side and allowing a reduction of the receiver complexity without any performance degradation. The proposed technique effectively alleviates the effects of ISI, ICI and improves CIR performance.

REFERENCES:


